



Problem 1 (Probability Theory).

1. Calculate the sample covariance between X and Y in the following data (one observation per row).

X	Y
9	1
3	-9
1	-1
4	3
10	-9
5	-1
9	-3
3	-10
10	-4
3	-2

- 2. What would be the new value for the sample covariance if:
 - Column X was multiplied by 0.5?
 - Column Y was replaced by a value 2c 0.5, where c is a constant that is fixed for all Y.

Problem 2 (Probabilities). What are the canonical parameters associated with the following probability distributions?

• Uniform

• Binomial

• Gaussian

• Bernoulli

• Exponential

Problem 3 (Probabilities). Let X_1 and X_2 be two independent binary random variables with $Pr(X_1 = 1) = 0.8$ and $Pr(X_2 = 1) = 0.5$. Let Y be their sum, $Y = X_1 + X_2$.

- 1. What is $\mathbb{E}(X_1)$?
- 2. What is $\mathbb{E}(Y)$?
- 3. What is $\mathbb{E}(Y \mid X_2 = 0)$?

Problem 4 (Analysis). What do the following functions converge to?

1.
$$f(x) = x/(1-x)$$
 for $x \to \infty$

2.
$$f(x) = \frac{x^2 - 4}{x - 2}$$
 for $x \to 2$

3.
$$f(x) = (n+1)x/x^n$$
 for $n > 1$ and for $x \to \infty$

4.
$$f(k) = \sum_{i=1}^{k} (1/2)^k$$
 for $k \to \infty$

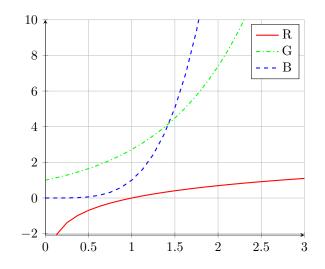
Problem 5 (Analysis).

Mark which of the following three functions correspond to which of the lines in the plot below.



2.
$$f(x) = x^4$$

3.
$$f(x) = \ln(x)$$



Problem 6 (Combinatronics).

1. How many different subsets does a set of size n have?

2. How many different subsets of size k does a set of size n have?

Problem 7 (Linear Algebra).

How many solutions are there for each of the given system equations? Why?

a)
$$2x + y = 1$$
$$5x - 2y = 3$$

b)
$$3u - 5v + 2w = 10$$

 $2u - 3v + 7w = 23$

c)
$$3p + 5q - r = 1$$

 $-p + 4q + 2r = 9$
 $6p + 10q - 2r = 3$

Problem 8 (Linear Algebra). Consider the following vectors.

1. What are the dimensions of each vector?

(a)
$$x_a = \begin{pmatrix} 4\\2\\-5 \end{pmatrix}$$

(c)
$$x_c = \begin{pmatrix} 5 \\ 0 \end{pmatrix}$$

(e)
$$x_e = \begin{pmatrix} 0 \\ 2 \end{pmatrix}$$

(b)
$$x_b = \begin{pmatrix} 3 \\ -1 \\ 1 \end{pmatrix}$$

$$(\mathbf{d}) \ x_d = \begin{pmatrix} 1 \\ 1 \\ 4 \\ 2 \end{pmatrix}$$

$$(f) x_f = \begin{pmatrix} -1\\1\\1\\-2 \end{pmatrix}$$

2. Perform the following vector operations using the vectors specified in Part. 1.

Elements of Machine Learning, WS 2022/2023

Jilles Vreeken and Aleksandar Bojchevski

Exercise Sheet #0: Self Assessment





(a) $x_a + x_c$

(c) $x_d \cdot x_f$

(b) $4 \cdot x_e$

- (d) $||x_d||$
- 3. Which pair of vectors in Part. 1 are orthogonal?

Problem 9 (Programming).

The purpose of this exercise is to familiarise yourself with the programming environment used for this course. For the needs of this exercise download and unpack the accompanying zipped data here.

- 1. Ensure that you have a working *python* environment including an option for editing and running *jupyter* notebooks. For this you may consult the instructions in the course site.
- 2. Familiarise yourselves with the python language, to be able to use
 - native data structures
 - function and class declarations
 - execution flow control (for, if, while), and also
 - comprehensions (for generators, lists, and dicts).

In this task you might find helpful the introductory notebook a0_notebook9.2 that we provide; open it in your environment and study its sample source code.

If you are already familiar with these, you may skip this question.

- 3. Familiarise yourselves with ML-related operations, until you are able to use
 - numpy arrays creation
 - numpy array indexing
 - vectorised operations on numpy arrays (sum, mean, comparisons, etc), as well as
 - matrix operations (dot, matrix multiplication).

Proceed with basic plotting using the standard matplotlib package, including

- \bullet line plots
- scatter plots, and
- bar plots.

In this task you might find helpful the introductory notebook a0_notebook9.3 that we provide; open it in your environment and study its sample source code.

If you are already familiar with these, you may skip this question.

- 4. Proceed with tabular data operations using the pandas package. For this you may follow the official 10 minute tutorial here.
- 5. Perform some basic data analysis.

Open notebook a0_notebook9.5 in your environment and complete the source code in the indicated cells.

Note: You do not need to submit the resulting notebook for this self-assessment assignment; in the future, however, you will be asked to provide your completed notebook, including a printout of it as a pdf file.